•	ttenuation measurement uncertainties caused by speckle	
S	tatistics	
	Kevin J. Parker	
	Department of Electrical Engineering, University of Rochester, Rochester, New York 14627	
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×	$\underline{n}_{r}(\mathbf{r}) = \frac{A}{1} \int e^{j2k_{0}\mathbf{n}\cdot\mathbf{r}'} \gamma(\mathbf{r}') dn' $ (1)	expression to evaluate the magnitude of backscattered pres-	
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<u>.</u>	where $A$ is a complex factor dependent on frequency, medi- um density, and amplitude of the incident wave; $v'$ represents the sample volume of integration: and <b>n</b> is a unit vector	we have $ p_{bs}(d) _{i} = [A_{0}e^{-2ad}/(r_{0}+d)]p_{i,d}$ , (8)	
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noise-to-signal	log expansion,	enabling	continued	use of
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	$\overline{\mathbf{x}}$
	more, the last expression shows that the variability in back- Combining Eqs. (22), (21), and (20) produces the de-
	scattered pressure, originally proportional to the mean back- sired result:
	southered processing is transformed to a constant in the last
	scattered pressure, is transformed to a constant in the log 0.44 (22)
	variable domain. This concept is illustrated in Fig. 1(a) and $\sigma_{-} = \frac{0.11}{2}$ . (23)
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The variance of a least-squares estimate for the slope b can now be written as<sup>17,18</sup>

$$\sigma_b^2 = \frac{\sigma_y^2}{\left[\sum_{j=1}^{M} (X_j - \overline{X})^2\right]},$$
 (21)

where there are M independent sample volume depths for which data are obtained. Assuming the sample volumes are oppositively desmarin the martine . . г.

which shows that the expected variability or error in attenuation measurement is a constant which depends on the number and spacing of the sample volumes, not on the material backscatter coefficient (the mean value a of the Rayleigh statistics) or the magnitude of attenuation. Thus the fractional error in attenuation  $\sigma_{\alpha}/\alpha$  decreases with increasing frequency, as shown in Fig. 1(c).

When the value of attenuation is measured at Findepen-

ful approximation we have from least-squares error analy-sis<sup>17,18</sup>

$$\sigma_{a'}^2 = \sigma_{y'}^2 \left\{ \frac{\sum \ln^2(f_i)}{F \sum \left[ \ln(f_i) - \overline{\ln(f)} \right]^2} \right\},\tag{32}$$

Occurrences

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	where the summation is over discrete frequ Using the small error approximation of E	Lencies $i = 1$ to $F$ .		
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(a)	Whereas projecting to 1 MHz to find $\alpha_0$ , using Eq. (33).
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	#2	identical attenuation magnitudes near the mean frequency, tend to cluster along a reciprocal or hyperbolic shaped
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$\Delta f \cong 1/\Delta t = C/2\Delta X.$	(48) t	he results of Eq. (52), yields:	
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	Am. 65, 512–517 (1979). <sup>2</sup> K. J. Parker and T. A. Tuthill, "CCl <sub>4</sub> induced changes in ultrasonic prop-	ments," IEEE Trans. Sonics Ultrason. SU-31, 313–329 (1984). <sup>11</sup> R. Kuc, "Estimating reflected ultrasound spectra from quantized sig-	
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